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# Nuclear quadrupole interactions of ${ }^{11} \mathrm{~B}$ in a $\mathrm{LiB}_{3} \mathrm{O}_{5}$ single crystal 

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#### Abstract

The rotation patterns of the nuclear magnetic resonance (NMR) spectra of an ${ }^{11} \mathrm{~B}$ nucleus in a $\mathrm{LiB}_{3} \mathrm{O}_{5}$ (LBO) single crystal were measured in the three mutually perpendicular crystallographic planes at room temperature. We identified three centres denoted as B1, B2, and B3, each of which consists of four sets of ${ }^{11} \mathrm{~B}$ NMR spectra originating from the chemically equivalent but magnetically inequivalent sites. The four sets belonging to each centre were properly classified in accordance with crystal symmetry and analysed. The principal values and principal axis orientations of the nuclear quadrupole coupling (NQC) tensors were determined for the first time. The centres B1, B2, and B3 were assigned to boron sites in the crystalline lattice of LBO by comparing the directions of the B-O bonds and the principal axes of the NQC tensor ( $\mathbf{P}$ ). The NQC constant $\left(e^{2} q Q / h\right)$ and asymmetry parameter $(\eta)$ were determined as follows: for $\mathrm{B} 1, e^{2} q Q / h=2.615 \pm 0.005 \mathrm{MHz}$ and $\eta=0.266 \pm 0.005$; for $\mathrm{B} 2, e^{2} q Q / h=0.176 \pm 0.003 \mathrm{MHz}$ and $\eta=0.584 \pm 0.003$; and for B3, $e^{2} q Q / h=2.690 \pm 0.004 \mathrm{MHz}$ and $\eta=0.204 \pm 0.003$.


## 1. Introduction

Lithium triborate $\left(\mathrm{LiB}_{3} \mathrm{O}_{5}, \mathrm{LBO}\right)$ crystals possess some excellent qualities, such as chemical stability, high damage threshold, small dielectric constant, and transparency far into the ultraviolet [1-3]. More than anything else, this boron oxide compound has a nonlinear optical (NLO) coefficient much larger than that of $\mathrm{KTiOPO}_{4}$, which is another excellent NLO crystal discovered earlier. It has been shown that LBO is especially advantageous in the frequency conversion of high-power pulsed lasers [4, 5]. Practical applications for laser systems require radiation stability. Radaev et al [6] have shown that LBO meets the requirement in contrast

[^0]to such well-known materials as $\mathrm{KH}_{2} \mathrm{PO}_{4}, \mathrm{LiNbO}_{3}, \mathrm{Ba}_{2} \mathrm{NaNb}_{5} \mathrm{O}_{15}$, and $\mathrm{KTiOPO}_{4}$. There are only a relatively small number of studies on the nuclear magnetic resonance (NMR) of LBO. Matsuo et al $[7,8]$ studied the ${ }^{7} \mathrm{Li}$ nuclear relaxation and line intensities as a function of temperature on both the crystal and glass phases of LBO. The nuclear quadrupole coupling (NQC) constant $e^{2} q Q / h$ and the asymmetry parameter $\eta$ of both ${ }^{7} \mathrm{Li}$ and ${ }^{11} \mathrm{~B}$ in LBO were evaluated in our previous report [9].

In this work, we study the local structure around the boron atoms by investigating the quadrupole interactions of the ${ }^{11} \mathrm{~B}$ nucleus in LBO. The quadrupole Hamiltonian parameters are more precisely determined than those in our previous report [9] by employing a sample with better quality and by achieving more accurate sample alignment. From the angular rotation patterns of ${ }^{11} \mathrm{~B}$ NMR measured at room temperature, the principal values and principal axis orientations of NQC tensors are determined. The chemical bonding structure of B-O in LBO is discussed in terms of the present results and the electron-density-deformation (EDD) peak previously reported by others [3].

## 2. Crystal structure

The crystal structure of LBO was initially determined by König and Hoppe [10] and later verified by Shuqing et al [11]. It crystallizes in the form of orthorhombic space group Pna2 $1_{1}$ belonging to the point group $m m 2$. A unit cell of this crystal contains four formula units and has lattice parameters $a=0.8447 \mathrm{~nm}, b=0.73789 \mathrm{~nm}$, and $c=0.51408 \mathrm{~nm}$ [3]. The symmetry elements of $P n a 2_{1}$ are characterized by two glide planes and one screw axis, and there are four chemically equivalent but magnetically inequivalent sites for each crystallographically distinct atom.

Figure 1 shows the scheme of a set of $\mathrm{B}_{3} \mathrm{O}_{7}$ bonds, i.e. the three crystallographically distinct borons and the nearest oxygens surrounding the borons, and the ion positions are listed in table 1. The crystallographically distinct atoms are distinguished using the arabic numerals in parentheses. The main structural unit of LBO consists of two crystallographically distinct boron-oxygen triangles and one boron-oxygen tetrahedron. The $\mathrm{B}(1)$ atom lies almost within the planar triangles formed by the oxygens $O(1), O(2)^{i}$, and $O(3)$, and the $B(3)$ atom by $\mathrm{O}(3), \mathrm{O}(4)^{\mathrm{iii}}$, and $\mathrm{O}(5)^{\mathrm{v}}$. The two triangles possess a common vertex, the $\mathrm{O}(3)$ atom. On the other hand, the $\mathrm{B}(2)$ atom lies within the distorted tetrahedron surrounded by oxygens $\mathrm{O}(1)$, $\mathrm{O}(2), \mathrm{O}(4)^{\mathrm{iiii}}$, and $\mathrm{O}(5)^{\mathrm{iv}}$. The $\mathrm{B}(2)$ atom is linked to the $\mathrm{B}(1)$ and $\mathrm{B}(3)$ via $\mathrm{O}(1)$ and $\mathrm{O}(4)^{\mathrm{iii}}$, respectively, and the Li atom is in the channel along the $c$ axis. The boron sites as shown in figure 1 and listed in table 1 will be adopted as the representative site I among four chemically equivalent sites I to IV.

## 3. Experimental procedure

The LBO single crystals used in the present study were synthesized by the top seeded slow cooling method [1] at CASIX in China. In order to measure the angular dependence of the NMR spectra, a crystal sample was oriented by obtaining a number of x-ray-diffraction patterns. The sample was subsequently sawn with the faces perpendicular to the crystal axes $a, b$, and $c$, which are high symmetry directions. NMR spectra were taken from the as-grown LBO sample $3.0 \times 4.0 \times 5.0 \mathrm{~mm}^{3}$ along the $a, b$, and $c$ axes, respectively.

The angular dependences of the NMR spectra were measured at room temperature by employing an MSL 200S pulsed NMR spectrometer, operating at a static magnetic field of 4.7 T. A single pulse, having width $1 \mu \mathrm{~s}$, was used. The repetition time and the ring down delay time were about 10 min and $6 \mu \mathrm{~s}$, respectively. The carrier frequency of the pulse was


Figure 1. Practical scheme of three crystallographically distinct borons together with their nearest oxygens in the $\mathrm{LiB}_{3} \mathrm{O}_{5}$ lattice, showing the crystallogaphic axes $\mathbf{a}, \mathbf{b}$, and $\mathbf{c}$. Each of $\mathbf{a}, \mathbf{b}$, and c corresponds to one eighth of its lattice constant, respectively. (See the footnote in table 1 for the meaning of the superscript symmetry codes.) The principal axes of the $\mathbf{P}$ tensor for centres $B 1$, $B 2$, and $B 3$ (see text) have been represented as vectors with origins at $B(1), B(2)$, and $B(3)$, respectively.

Table 1. Ion positions of three crystallographically distinctive borons $\mathrm{B}(1), \mathrm{B}(3)$, and $\mathrm{B}(2)$ and the nearest oxygens around the respective boron are given in units of $a, b$, and $c$ lattice parameters in $\mathrm{LiB}_{3} \mathrm{O}_{5}$. (Taken from [3], except for five different choices of oxygens which were obtained from the original data by applying the superscript symmetry codes.)

| Atoms $^{\mathrm{a}}$ | $x / a$ | $y / b$ | $z / c$ |
| :--- | ---: | ---: | ---: |
| $\mathrm{~B}(1) \mathrm{O}_{3}$ triangle |  |  |  |
| $\mathrm{B}(1)$ | 0.00968 | 0.66439 | 0.8098 |
| $\mathrm{O}(1)$ | 0.08644 | 0.50430 | 0.8022 |
| $\mathrm{O}(2)^{\mathrm{i}}$ | -0.11633 | 0.70490 | 0.6535 |
| $\mathrm{O}(3)$ | 0.05809 | 0.79816 | 0.9848 |
| $\mathrm{~B}(3) \mathrm{O}_{3}$ triangle |  |  |  |
| $\mathrm{B}(3)$ | 0.15705 | 0.74859 | 0.1895 |
| $\mathrm{O}(3)$ | 0.05809 | 0.79816 | -0.0152 |
| $\mathrm{O}(4)^{\mathrm{iii}}$ | 0.23898 | 0.59024 | 0.1902 |
| $\mathrm{O}(5)^{\mathrm{v}}$ | 0.16102 | 0.87496 | 0.3840 |
|  |  |  |  |
| $\mathrm{~B}(2) \mathrm{O}_{4}$ tetrahedron |  |  |  |
| $\mathrm{B}(2)$ | 0.19437 | 0.44327 | 0.0063 |
| $\mathrm{O}(1)$ | 0.08644 | 0.50430 | -0.1978 |
| $\mathrm{O}(2)$ | 0.11633 | 0.29510 | 0.1535 |
| $\mathrm{O}(4)^{\text {iii }}$ | 0.23898 | 0.59024 | 0.1902 |
| $\mathrm{O}(5)^{\text {iv }}$ | 0.33898 | 0.37496 | -0.1160 |

${ }^{\text {a }}$ Symmetry codes: (i) $-x, 1-y, \frac{1}{2}+z$; (iii) $\frac{1}{2}-x, \frac{1}{2}+y,-\frac{1}{2}+z$; (iv) $-\frac{1}{2}+x, \frac{1}{2}-y,-1+z$; (v) $1-x, 1-y,-\frac{1}{2}+z$
varied in the range of $\omega_{0} / 2 \pi=63.2-65.2 \mathrm{MHz}$ in order to excite all the satellite lines of ${ }^{11} \mathrm{~B}$ NMR. The Larmor frequency of the ${ }^{11} \mathrm{~B}$ nucleus was 64.2 MHz at the magnetic field $\mathbf{B}$ used for the experiment. The crystal alignments have been established within $\pm 0.2^{\circ}$ in the three


Figure 2. Angular dependence of the NMR spectra of the B1 and B3 centres observed at room temperature in the three crystallographic planes $a b, b c$, and $c a$ of the $\mathrm{LiB}_{3} \mathrm{O}_{5}$ single crystal. The experimental NMR lines are represented by closed circles and squares while the solid curves for B1 and dotted curves for B3 are calculated ones using the EFG matrix in table 3.
planes by adjusting the crystal orientation in such a way as to achieve pairwise degeneracy of the NMR spectra arising from four chemically equivalent boron sites. The NMR spectra were recorded by varying the orientation of $\mathbf{B}$ in the three planes in steps of $5.0^{\circ}$ with polar $\vartheta$ and the azimuthal angle $\phi$ ranging from $0^{\circ}$ to $180^{\circ}$.

## 4. Results and discussion

The isotope ${ }^{11} \mathrm{~B}$ is a quadrupolar nucleus with nuclear spin $I=3 / 2$ and natural abundance of $80.42 \%$. When the quadrupolar nucleus is located in the surroundings of the non-zero electric field gradient (EFG), it gives $2 I$ resonance lines for the case where the nuclear quadrupole interaction perturbs the nuclear Zeeman energy levels. One of them is the central transition line $(|1 / 2\rangle \leftrightarrow|-1 / 2\rangle)$ and the other two are satellite ones $(|3 / 2\rangle \leftrightarrow|1 / 2\rangle$ and $|-3 / 2\rangle \leftrightarrow|-1 / 2\rangle)$. From the angular dependence of the NMR spectra, the three transitions between the nuclear spin states were clearly identified in the planes $a b, b c$, and $c a$ as shown in figures 2 and 3. For an arbitrary direction of the magnetic field with respect to the crystal axes and planes, there are four sets of NMR lines arising from four chemically equivalent boron sites. If the magnetic field is restricted to the planes $a b, b c$, and $c a$, the four sets are pairwise degenerate and only two sets of NMR lines are observed. The non-degenerate pairs have mirror symmetry about the axes $a, b$, and $c$ in each of the planes $a b, b c$, and $c a$. Finally, all four sets are completely merged into one when the magnetic field is along any of the $a, b$, and $c$ axes.

The observable number of NMR spectra for a particular nucleus in LBO crystals is primarily determined by the symmetry of the point group $m m 2$. However, the number is reduced when $\mathbf{B}$ is applied to a certain orientation in which the apparent magnetic symmetry is higher than that of the point group of the crystal lattice. Consequently, the pairs of sites, having twofold symmetry about the $c$ axis and mirror symmetry across the $b c$ and $c a$ planes, become identical for $\mathbf{B}$ applied in the $a b, b c$, and $c a$ planes, respectively. When $\mathbf{B}$ is applied parallel to each crystallographic axis, all four sites in mm 2 become magnetically identical. However, all sites are magnetically distinct for $\mathbf{B}$ applied on skew planes which deviate from


Figure 3. Angular dependence of the NMR spectrum of the $B 2$ centre observed at room temperature in the three crystallographic planes $a b, b c$, and $c a$ of the $\mathrm{LiB}_{3} \mathrm{O}_{5}$ single crystal. The experimental NMR lines are represented by closed circles and squares while the solid curves are calculated ones using the EFG matrix in table 3.

Table 2. Degenerate pairs, magnetic symmetry elements, and observable sets of NMR spectra arising from chemically equivalent sites I-IV.

| Orientations of B | Degenerate pairs of NMR spectra | Magnetic symmetry elements | Observable sets of spectra |
| :---: | :---: | :---: | :---: |
| $a, b, c$ axes | $\mathrm{S}_{\text {I }}, \mathrm{S}_{\text {II }}, \mathrm{S}_{\text {III }}, \mathrm{S}_{\text {IV }}$ |  | 1 |
| $a b$ plane | $\mathrm{S}_{\text {I }}, \mathrm{S}_{\text {IV }} / \mathrm{S}_{\text {III }}, \mathrm{S}_{\text {III }}$ | $2 \\| c($ or $m \perp a$ and $b)$ | 2 |
| $b c$ plane | $\mathrm{S}_{\text {I }}, \mathrm{S}_{\text {III }} / \mathrm{S}_{\text {III }}, \mathrm{S}_{\text {IV }}$ | $m \perp a$ | 2 |
| ca plane | $\mathrm{S}_{\mathrm{I}}, \mathrm{S}_{\text {II }} / \mathrm{S}_{\text {III }}, \mathrm{S}_{\text {IV }}$ | $m \perp b$ | 2 |
| Otherwise | None |  | 4 |

the exact crystallographic planes. The degenerate aspects and the observable sets of NMR spectra $\mathrm{S}_{\mathrm{I}}-\mathrm{S}_{\text {IV }}$ arising from the respective sites I-IV are listed in table 2 . The results are well in accord with those of NMR spectra as shown in figures 2 and 3.

In the case of a point defect located in a crystal lattice of the point group $m m 2$, the degenerate aspects are also applicable to EPR spectra. Previously we obtained the same degenerate aspects of EPR spectra for four $\mathrm{Cr}^{3+}$ [12-14] and four $\mathrm{Fe}^{3+}$ [14-16] centres in $\mathrm{KTiOPO}_{4}$ crystals with the same point group $m m 2$ as that of LBO. The degenerate aspects are applicable to both NMR and EPR spectra and can be used as indicators for properly classifying the spectra originating from chemically equivalent but magnetically inequivalent sites and for examining the equivalency between several centres with similar NMR parameters due to very similar environments around the nuclei.

For the analysis of NMR spectra and their angular dependence, the Hamiltonian for an $I=3 / 2$ nucleus system is:

$$
\begin{equation*}
H=H_{\mathrm{Z}}+H_{\mathrm{Q}} \tag{1}
\end{equation*}
$$

where $H_{\mathrm{Z}}$ is the nuclear Zeeman term and $H_{\mathrm{Q}}$ the nuclear quadrupole interaction. The $H_{\mathrm{Q}}$ is expressed as follows:

$$
\begin{equation*}
H_{\mathrm{Q}}=\mathbf{I} \cdot \mathbf{P} \cdot \mathbf{I} \tag{2}
\end{equation*}
$$

by introducing the nuclear spin operator $\mathbf{I}$ and the NQC tensor $\mathbf{P}$ [17]. The $\mathbf{P}$ matrix is
symmetric and traceless and given by

$$
\mathbf{P}=P\left(\begin{array}{ccc}
\eta-1 & 0 & 0  \tag{3}\\
0 & -\eta-1 & 0 \\
0 & 0 & 2
\end{array}\right)
$$

in the principal axis $\operatorname{system}(x, y, z)$, where

$$
\begin{equation*}
P=\frac{e^{2} q Q}{4 I(2 I-1)} \tag{4}
\end{equation*}
$$

The $e^{2} q Q / h$ is the NQC constant and the $\eta$ is the asymmetry parameter. Since the nuclear spin of ${ }^{11} \mathrm{~B}$ is $3 / 2, P=e^{2} q Q / 12$. The parameter $e q$ is just the EFG of largest magnitude $\left(V_{z z}\right)$, and $e Q$ describes the electrical shape of the nucleus and is a fixed number. By employing the EPR-NMR program which adapted the diagonalization algorithm of the $\mathbf{P}$ matrix representation of the Hamiltonian [18], we have determined the principal values and the principal axis orientations of the $\mathbf{P}$ tensor.

There are two possibilities for choosing a set of spectra in each of the planes $a b, b c$, and $c a$ (see figures 2 and 3). Therefore, there are eight different ways to assign a set of spectra arising from four chemically equivalent ${ }^{11} \mathrm{~B}$ sites in the three crystallographic planes. The agreement of the calculated NMR line positions with experimental ones is excellent for four particular choices of the spectra, while it fails completely for the others. The four sets corresponding to the good choices are defined as the centres B1 (i) and B3(i) as shown in figure 2, and B2(i) in figure 3. The variables in parentheses $i=\mathrm{I}$, II, III, IV indicate NMR spectra arising from four chemically equivalent boron sites as listed in table 2 . The four sets yield the identical principal values of $\mathbf{P}$ tensors, whereas the orientations of the principal axes are different for each set. The rotation matrices, which transform the data of all symmetry-related sites into those of a reference site, could be found from the crystal symmetry of LBO. To obtain an accurate and meaningful determination of NMR parameters, a simultaneous fitting of all the experimental data set for chemically equivalent sites was carried out using the rotation matrices [18].

The final best fit of the principal values of the $\mathbf{P}$ tensors and the principal axes with respect to the crystallographic axes, $a, b, c$ are listed in table 3 for the representative spectra B1(I), B3(I), and B2(I). The principal axis systems have been chosen to follow the convention $\left|P_{x x}\right| \leqslant\left|P_{y y}\right| \leqslant\left|P_{z z}\right|$, and have been represented in the right-handed coordinate system. The NQC constant and asymmetry parameter obtained from the principal values of the $\mathbf{P}$ tensor using equations (3) and (4) are also listed. The $e^{2} q Q / h$ of the centre B 1 is very similar to that of the centre B3 but approximately 14 times greater than that of the B2 centre.

To assign the centres $\mathrm{B} 1, \mathrm{~B} 2$, and B 3 to boron sites in the LBO crystal lattice, we have compared all four sets of the principal axes $x, y$, and $z$ of the $\mathbf{P}$ tensor belonging to each centre with the B-O bond directions of LBO using the crystallographic data in table 1. One set of the spectra belonging to each centre, and providing a good match to the directions of the $\mathrm{B}-\mathrm{O}$ bond, is selected as representative of $\mathrm{B} 1(\mathrm{I}), \mathrm{B} 3(\mathrm{I})$, and $\mathrm{B} 2(\mathrm{I})$ as listed in tables 3 and 4. The principal $x$ axis of both the centres B 1 and B 3 nearly coincides with the longest bond $\mathrm{B}(1)-$ $\mathrm{O}(3)$ in $\mathrm{B}(1) \mathrm{O}_{3}$ and $\mathrm{B}(3)-\mathrm{O}(3)$ in $\mathrm{B}(1) \mathrm{O}_{3}$ planar triangles with $5.4^{\circ}$ and $1.0^{\circ}$ of the deviation angle $(\Delta \vartheta)$, respectively. The asymmetry parameter $\eta$ is expressed by $\left|P_{x x}-P_{y y}\right| /\left|P_{z z}\right|$ from equation (3) or $\left|V_{x x}-V_{y y}\right| /\left|V_{z z}\right|$ in the principal axis system of the EFG tensor, where $\left|P_{z z}\right|=(e Q / 6)\left|V_{z z}\right|$ with the convention $\left|V_{x x}\right| \leqslant\left|V_{y y}\right| \leqslant\left|V_{z z}\right|$. Since the parameter $e Q$ is a fixed number, each principal value ( $P_{i i}, i i=x x, y y, z z$ ) is proportional to that ( $V_{i i}$ ) of the EFG tensor. Therefore, the coincidence between the $x$ axis with the smallest principal value of $\mathbf{P}$ and the longest B-O bond can be explained by the fact that the EFG is proportional to $1 / r^{3}$. The largest $\mathrm{O}(1)-\mathrm{B}(1)-\mathrm{O}(2)^{\mathrm{i}}$ and $\mathrm{O}(4)^{\mathrm{iii}}-\mathrm{B}(3)-\mathrm{O}(5)^{\mathrm{v}}$ bond angles, formed by the short bonds in the triangles, are $123.32^{\circ}$ and $124.92^{\circ}$, respectively. The smallest $\mathrm{O}(2)^{\mathrm{i}}-\mathrm{B}(1)-\mathrm{O}(3)$

Table 3. Principal values and principal axis directions of the $\mathbf{P}$ tensor in polar coordinates $(\theta, \phi)$ for the representative spectra of B1(I), B3(I), and B2(I), respectively. The quadrupole interaction parameters are also listed.

|  |  |  | Direction of principal axes |  |
| :--- | :--- | :--- | :---: | :---: |
| Centres |  | Principal values | $\theta(\mathrm{deg})$ | $\phi(\mathrm{deg})$ |
|  |  |  |  |  |
| B1(I) | $\left\|P_{x x}\right\|$ | $0.160 \pm 0.001 \mathrm{MHz}$ | 52.6 | 73.4 |
|  | $\left\|P_{y y}\right\|$ | $0.276 \pm 0.001 \mathrm{MHz}$ | 112.8 | 114.6 |
|  | $e^{2} q Q / h$ | $0.436 \pm 0.001 \mathrm{MHz}$ | 133.9 | 30.8 |
|  | $\eta$ | $2.615 \pm 0.005 \mathrm{MHz}$ |  |  |
|  | $\left\|P_{x x}\right\|$ | $0.266 \pm 0.005$ |  |  |
| B3(I) | $\left\|P_{y y}\right\|$ | $0.178 \pm 0.001 \mathrm{MHz}$ | 133.9 | 156.8 |
|  | $\left\|P_{z z}\right\|$ | $0.448 \pm 0.001 \mathrm{MHz}$ | 63.3 | 103.4 |
|  | $e^{2} q Q / h$ | $2.690 \pm 0.004 \mathrm{MHz}$ | 117.5 | 28.6 |
|  | $\eta$ | $0.204 \pm 0.003$ |  |  |
|  | $\left\|P_{x x}\right\|$ | $0.006 \pm 0.001 \mathrm{MHz}$ | 127.8 | 172.8 |
| B2(I) | $\left\|P_{y y}\right\|$ | $0.023 \pm 0.001 \mathrm{MHz}$ | 59.8 | 236.0 |
|  | $\left\|P_{z z}\right\|$ | $0.029 \pm 0.001 \mathrm{MHz}$ | 127.6 | 229.4 |
|  | $e^{2} q Q / h$ | $0.176 \pm 0.003 \mathrm{MHz}$ |  |  |
|  | $\eta$ | $0.584 \pm 0.003$ |  |  |

and $\mathrm{O}(3)-\mathrm{B}(3)-\mathrm{O}(5)^{\mathrm{v}}$ bond angles are $116.87^{\circ}$ and $112.84^{\circ}$, respectively. The bond angles deviate slightly from the $120^{\circ}$ formed by an isosceles triangle. If the triangles formed by the oxygens $\mathrm{O}(1), \mathrm{O}(2)^{\mathrm{i}}$, and $\mathrm{O}(3)$ as well as $\mathrm{O}(3), \mathrm{O}(4)^{\mathrm{iii}}$, and $\mathrm{O}(5)^{\mathrm{v}}$ are isosceles, one of the principal axis directions will point to the normal of the triangular plane as observed in other crystals [19, 20] and calculations [21]. Such a normal direction of the $\mathrm{B}(1) \mathrm{O}_{3}$ and $\mathrm{B}(3) \mathrm{O}_{3}$ triangle provides a good match with the principal $z$ axis of B 1 and B 3 with $\Delta \vartheta=0.4^{\circ}$ and $2.0^{\circ}$, respectively. In the two triangles, the longest and shortest bonds exist only in $\mathrm{B}(1) \mathrm{O}_{3}$ rather than $\mathrm{B}(3) \mathrm{O}_{3}$. Therefore, the $\mathrm{B}(1) \mathrm{O}_{3}$ triangle is more asymmetric than that of the $\mathrm{B}(3) \mathrm{O}_{3}$, and the $\mathrm{B}(1)$ yields a larger asymmetry parameter $(\eta=0.266)$ than that $(\eta=0.204)$ of $\mathrm{B}(3)$, as listed in table 3. The smaller $P_{x x}(0.160 \mathrm{MHz})$ of B1 than that $(0.178 \mathrm{MHz})$ of B3 is also in good agreement with EFG $\sim 1 / r^{3}$. Since $e^{2} q Q / h=12\left|P_{x x}\right| /(\eta-1) h$ from equations (3) and (4), the larger value of $e^{2} q Q / h$ for B3 can be understood from the fact that the larger $\left|P_{x x}\right|$ value of B 3 overcomes the smaller values of $\eta$ than those of B 1 . On the basis of the overall present NMR results, we have reached the conclusion that the centres B1 and B3 arise from the $B(1)$ and $B(3)$ boron site in LBO, respectively.

The bond angle of $112.94^{\circ}$ formed by $\mathrm{O}(1)-\mathrm{B}(2)-\mathrm{O}(4)^{\mathrm{iii}}$ is the largest for the distorted tetrahedron. The others range from $108.4^{\circ}$ to $109.6^{\circ}$ which are close to the typical angle $109.5^{\circ}$ for a perfect tetrahedron. If the tetrahedron were perfect with cubic symmetry, the nuclear quadrupole interaction would be zero. The small distortion from the perfect tetrahedron yields the non-zero NQC constant of $B(2)$, consequently its magnitude is much smaller than those of $\mathrm{B}(1)$ and $\mathrm{B}(3)$, as expected from the boron surroundings. The $x$ axis with the smallest principal value is usually directed to the longest bond for the three-coordinated B1 and B3 centres, but not for the case in the B 2 centre arising from the four-coordinated boron surroundings. One of the two long bonds, $\mathrm{B}(2)-\mathrm{O}(2)(0.14843 \mathrm{~nm})$, provides a good match to the principal $y$ axis with $\Delta \vartheta=2.5^{\circ}$ (see table 4).

Each $B(1)$ and $B(3)$ uses its $\mathrm{sp}^{2}$ hybrid orbitals with three valence electrons to form bonds with oxygen atoms, and $\mathrm{B}(2)$ lends its four $\mathrm{sp}^{3}$ hybrid orbitals with four oxygen atoms. It was

Table 4. Comparison of the $\mathrm{B}-\mathrm{O}$ bond and plane-normal directions in $\mathrm{B}(1) \mathrm{O}_{3}$ and $\mathrm{B}(3) \mathrm{O}_{3}$ triangles, and the $\mathrm{B}-\mathrm{O}$ bond in a $\mathrm{B}(2) \mathrm{O}_{4}$ tetrahedron with the principal axis directions of the $\mathbf{P}$ tensors for the representative spectra $\mathrm{B} 1(\mathrm{I}), \mathrm{B} 3(\mathrm{I})$, and $\mathrm{B} 2(\mathrm{I})$, respectively (see figure 1 ).

| Distances and directions in $\mathrm{B}(1) \mathrm{O}_{3}$ |  |  |  |  | Principal axes of B1(I) |  | Angle ${ }^{\text {a }}$ <br> $\Delta \vartheta(\mathrm{deg})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bond | $d(\mathrm{~nm})$ | $\theta$ (deg) | $\phi$ (deg) |  | $\theta$ (deg) | $\phi$ (deg) |  |
| $\mathrm{B}(1)-\mathrm{O}(3)$ | 0.13967 | 49.9 | 67.4 | $x$ | 52.6 | 73.4 | 5.4 |
| $\mathrm{B}(1)-\mathrm{O}(2)^{\mathrm{i}}$ | 0.13666 | 125.9 | 164.4 | y | 112.8 | 144.6 | 21.6 |
| Plane normal ${ }^{\text {b }}$ |  | 133.6 | 30.5 | z | 133.9 | 30.8 | 0.4 |
| $\mathrm{B}(1)-\mathrm{O}(1)$ | 0.13481 | 91.7 | 298.8 |  |  |  |  |
| Distances and directions in $\mathrm{B}(3) \mathrm{O}_{3}$ |  |  |  |  | Principal axes of B3(I) |  |  |
| Bond | $d(\mathrm{~nm})$ | $\theta$ (deg) | $\phi$ (deg) |  | $\theta$ (deg) | $\phi$ (deg) | $\Delta \vartheta(\mathrm{deg})$ |
| $\mathrm{B}(3)-\mathrm{O}(3)$ | 0.13930 | 139.0 | 156.4 | $x$ | 139.9 | 156.8 | 1.0 |
| $\mathrm{B}(3)-\mathrm{O}(5)^{\mathrm{v}}$ | 0.13675 | 43.0 | 87.9 | $y$ | 63.3 | 103.4 | 23.7 |
| Plane normal ${ }^{\text {c }}$ |  | 116.9 | 30.7 | $z$ | 117.5 | 28.6 | 2.0 |
| $\mathrm{B}(3)-\mathrm{O}(4)^{\text {iii }}$ | 0.13581 | 89.9 | 300.7 |  |  |  |  |
| Distances and directions in $\mathrm{B}(2) \mathrm{O}_{4}$ |  |  |  |  | Principal axes of B2(I) |  |  |
| Bond | $d$ ( nm ) | $\theta$ (deg) | $\phi$ (deg) |  | $\theta$ (deg) | $\phi$ (deg) | $\Delta \vartheta(\mathrm{deg})$ |
| $\mathrm{B}(2)-\mathrm{O}(1)$ | 0.14610 | 135.8 | 153.8 | $x$ | 127.8 | 172.8 | 16.2 |
| $\mathrm{B}(2)-\mathrm{O}(2)$ | 0.14843 | 59.4 | 238.8 | $y$ | 59.8 | 236.0 | 2.5 |
| $\mathrm{B}(2)-\mathrm{O}(5)^{\mathrm{iv}}$ | 0.14633 | 115.4 | 337.7 | $z$ | 127.6 | 299.4 | 34.6 |
| $\mathrm{B}(2)-\mathrm{O}(4)^{\text {iii }}$ | 0.14872 | 50.5 | 70.8 |  |  |  |  |

[^1]proposed from the investigation of the EDD peak [3] that a pure $\sigma$-type bond is not realized along the shortest $\mathrm{B}(1)-\mathrm{O}(1)$ or $\mathrm{B}(1)-\mathrm{O}(2)^{\mathrm{i}}$ in the $\mathrm{B}(1) \mathrm{O}_{3}$ triangle, whereas the shape of the EDD peak of the longest $B(1)-O(3)$ extends closely along the bond and the $B(1)-O(3)$ bond is predominantly $\sigma$-type. It was additionally concluded [3] that the shape of the EDD peak of $\mathrm{B}(3)-\mathrm{O}(3)$ extends almost along the bond and is more symmetrical than that of $\mathrm{B}(1)-\mathrm{O}(3)$ about the bond, and the bond is purely $\sigma$-type. This agrees with our results in table 4 that the deviation angle of the $\mathrm{B}(3)-\mathrm{O}(3)$ bond $\left(1.0^{\circ}\right)$ from the $x$ axis is approximately five times smaller than that of $\mathrm{B}(1)-\mathrm{O}(3)\left(5.4^{\circ}\right)$. On the other hand, it was also shown by Radaev et al [3] that the EDD peaks of two long $\mathrm{B}(2)-\mathrm{O}(2)$ and $\mathrm{B}(2)-\mathrm{O}(4)^{\text {iii }}$ bonds are more symmetrical about the bonds than those of the other two $\mathrm{B}(2)-\mathrm{O}(1)$ and $\mathrm{B}(2)-\mathrm{O}(5)^{\text {iv }}$ bonds. This is also in good agreement with our result that the $\mathrm{B}(2)-\mathrm{O}(2)$ bonds nearly coincide with the $y$ axis. We have reached the conclusion from the overall facts that the centre $B 2$ arises from the $B(2)$ boron sites in LBO.

## 5. Conclusion

The degenerate aspects of the NMR spectra in table 2 can be used as the following indicators: (i) for properly classifying the spectra arising from chemically equivalent sites; (ii) for examining the equivalency between several centres. The nuclear quadrupole interaction parameters were determined as follows: for $\mathrm{B} 1, e^{2} q Q / h=2.615 \pm 0.005 \mathrm{MHz}$ and $\eta=0.266 \pm 0.005$; for $\mathrm{B} 2, e^{2} q Q / h=0.176 \pm 0.003 \mathrm{MHz}$ and $\eta=0.584 \pm 0.003$;
and for B3, $e^{2} q Q / h=2.690 \pm 0.004 \mathrm{MHz}$ and $\eta=0.204 \pm 0.003$. The centres B1, B2, and B3 were assigned to boron sites in LBO by comparing the directions of the $\mathrm{B}-\mathrm{O}$ bonds and principal axes of $\mathbf{P}$ tensors. The present results support the chemical bonding structure suggested by Radaev et al that the longest $\mathrm{B}(1)-\mathrm{O}(3)$ bond is predominantly a $\sigma$-type bond and $\mathrm{B}(3)-\mathrm{O}(3)$ is an almost pure $\sigma$-type bond. The principal axes of the $\mathbf{P}$ tensors for $\mathrm{B} 1, \mathrm{~B} 2$, and B3 can be used as complementary data with the EDD peak to elucidate the $\mathrm{B}-\mathrm{O}$ bonding structures.

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## References

[1] Chen C, Wu Y, Jiang A, Wu B, You G, Li R and Lin S 1989 J. Opt. Soc. Am. B 6616
[2] Lin S, Sun Z, Wu B and Chen C 1990 J. Appl. Phys. 67634
[3] Radaev S F, Maximov B A and Simonov V I 1992 Acta Crystallogr. B 48154
[4] Wu B, Chen N and Chen C 1989 Opt. Lett. 141080
[5] Ebrahimzadel M, Robertson G and Dunn M H 1991 Opt. Lett. 16767
[6] Radaev S F, Muradyan L A, Malakhova L F, Rurak Y V and Simonov V I 1989 Sov. Phys.-Crystallogr. 34842
[7] Matsuo T, Shibasaki M, Katsumata T and Onoda Y 1994 Japan. J. Appl. Phys. 333913
[8] Matsuo T, Shibasaki M, Saito N and Katsumata T 1996 J. Appl. Phys. 791903
[9] Kim I G, Choh S H and Kim J N 1998 J. Korean Phys. Soc. 32 S669
[10] König H and Hoppe R 1989 Z. Anorg. Chem. 439842
[11] Shuqing Z, Chaoen H and Hongwu Z 1990 J. Cryst. Growth 99805
[12] Ahn S W, Choh S H and Kim J N 1995 J. Phys.: Condens. Matter 7667
[13] Ahn S W, Choh S H and Rudowicz C 1997 Appl. Magn. Reson. 12351
[14] Ahn S W and Choh S H 1999 J. Phys.: Condens. Matter 113193
[15] Ahn S W, Choh S H and Choi B C 1995 J. Phys.: Condens. Matter 79615
[16] Ahn S W and Choh S H 1998 J. Phys.: Condens. Matter 10341
[17] Weil J A, Bolton J R and Wertz J E 1994 Electron Paramagnetic Resonance (New York: Wiley) p 138
[18] Mombourquette M J, Weil J A and McGavin D G 1995 Operation Instructions for Computer Program EPR-NMR Ver. 6.0 University of Saskatchewan, Canada
[19] Maurer H M, Schmidt P C and Weiss A 1997 J. Mol. Struct. 41111
[20] Kim I G and Choh S H 1999 J. Phys.: Condens. Matter 118283
[21] Choh S H, Shin H W, Park I W, Ju H, Kim J H and Kim H J 2003 J. Magn. Reson. Sco. 716


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[^1]:    ${ }^{\text {a }}$ Angles between the $\mathrm{B}-\mathrm{O}$ bond or the plane-normal directions and the principal axis directions of the $\mathbf{P}$ tensor.
    ${ }^{\mathrm{b}}$ Normal direction to the face of the triangle formed by $\mathrm{O}(1), \mathrm{O}(2)^{\mathrm{i}}$, and $\mathrm{O}(3)$.
    ${ }^{\mathrm{c}}$ Normal direction to the face of the triangle formed by $\mathrm{O}(3), \mathrm{O}(4)^{\mathrm{iii}}$, and $\mathrm{O}(5)^{\mathrm{v}}$.

